

Set Theory

$\{1, 7, 2\} = \{1, 2, 7\} = \{2, 1, 2, 7\}$	set (also: multiset, bags)
1 ε{1,7,2} 3 ε{1,7,2}	element
$\{2,7\} \subset \{1,7,2\}$ $\{7,3\} \notin \{1,7,2\}$	subset

Set Theory

$\overline{A} = \{x: x \notin A\}$	complement
$A \cup B = \{x: x \in A \text{ or } x \in B\}$	union
$A \cap B = \{x: x \in A \text{ and } x \in B\}$	intersection
A - B = {x: $x \in A$ and $x \notin B$ }	difference
$\mathscr{P}(A) = \{B: B \text{ is subset of } A\}$	powerset

A x B = $\{(a,b): a \in A \text{ and } b \in B\}$ Cartesian Product

Inner Joins in SQL

equijoin

SELECT S.*, SG.* FROM student AS S, studentgroup AS SG WHERE S.SID = SG.PresidentID;

Explicit joins

SELECT S.*, SG.* FROM (student AS S JOIN studentgroup AS SG ON S.SID = SG.PresidentID);

join condition

University
• List students and courses they are enrolled in.

Outer Joins in SQL

SELECT S.*, SG.* FROM (student AS S LEFT OUTER JOIN studentgroup AS SG ON S.SID = SG.PresidentID);

SELECT S.*, SG.* FROM (student AS S RIGHT OUTER JOIN studentgroup AS SG ON S.SID = SG.PresidentID);

SELECT S.*, SG.* FROM (student AS S FULL OUTER JOIN studentgroup AS SG ON S.SID = SG.PresidentID);

> In Oracle • can drop OUTER • alternative notation using (+)

Join Examples

University

- List all students who are enrolled in courses.
- List all students and, if they are enrolled in a course, which courses they are enrolled in.

• List all students and what courses they are enrolled in; list students if they are not enrolled in any course and list courses even if there are no enrollments.

- List all students who are not enrolled in a course.
- List student groups without presidents.
- List students who are not president.

Set Operations



Intersection and Difference not supported in some systems (Access, SQLServer). Workaround later.

Set Operations Examples

University

- List student members of DeFrag and HerCTI.
- List students that are members of both DeFrag and HerCTI. • We only allow gaming students to join DeFrag; list students
- that violate this rule.We require that all gaming students are members of DeFrag;
- list students that violate this rule.
- List students that are not enrolled in any courses.
- · List students that are not presidents of any group.

Duplicates with Set Operations

Duplicates are eliminated if we use set operations like

UNION INTERSECT EXCEPT

(union) (intersection) (set difference)

Adding the keyword ALL retains duplicated:

UNION ALL INTERSECT ALL EXCEPT ALL

Only UNION ALL is supported in Oracle.

Set Operations Using Joins

Example:

All employees who are instructors or staff.

SELECT E.* FROM employee AS E, instructor AS I, staff AS S WHERE E.ID = I.ID or E.ID = S.ID

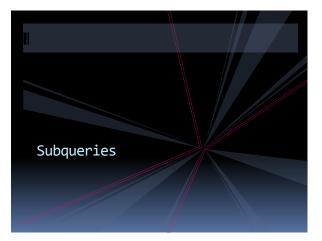
Set Operations Using Joins

Example:

All employees who are instructors or staff.

SELECT E.* FROM employee AS E, instructor AS I, staff AS S WHERE E.ID = I.ID or E.ID = S.ID

Is $E \cap (I \cup S)$ the same as $E \times I \times S$ restricted to tuples where E.ID = I.ID or E.ID = S.ID ?



The IN Operator

Conditions can contain IN for "element of"

SELECT LastName, FirstName FROM student WHERE started IN (2010, 2013, 2014);

SELECT LastName, FirstName FROM student WHERE started NOT IN (2010, 2013, 2014);

SELECT Department, CourseName FROM Course WHERE Department IN ('CSC', 'TT', 'IS');

The IN Operator

SELECT * FROM enrolled WHERE (Quarter, Year) in (('Fall', 2012), ('Winter', 2012));

This will not work in many systems (e.g. Access). Can redo as OR of ANDS.

Nesting Queries with IN

SELECT LastName, FirstName, SID FROM student WHERE SID IN (SELECT PresidentID FROM studentgroup)

In Examples

• List all students enrolled in a computer science course. • List all students who are members of HerCTI.

• List undergraduate computer science students.

• Presidents who are members of their groups.

Excursion: Using IN for set operations

Set Intersection

Example: Presidents that were enrolled in 2013.

SELECT LastName, FirstName, SID FROM student WHERE sid IN (SELECT presidentID FROM studentgroup) AND sid IN (SELECT studentID FROM enrolled WHERE year = 2013);

• Students who enrolled in both 2005 and 2006.

Set Complement

Example: Students who did not enroll in 2013.

SELECT LastName, FirstName, SID FROM student WHERE sid NOT IN (SELECT studentID FROM enrolled WHERE year = 2013);

· Presidents who are not members of their groups.

Set Difference

Example: Students who are presidents but not members of any group.

SELECT LastName, FirstName, SID FROM student WHERE sid IN (SELECT presidentID FROM studentgroup) AND sid NOT IN (SELECT studentID FROM memberof);

• CS students who are enrolled in a course, but no CS course.

Set UNION and OR

compare to

(SELECT studentID FROM memberof) UNION (SELECT presidentID FROM studentgroup); (SELECT LastName, FirstName, SID FROM student WHERE sid IN (SELECT studentID FROM memberof) OR sid IN (SELECT presidentID FROM studentgroup);

Set Operations Examples

• List students who have a mentor who is a president of a studentgroup.

• List courses that exist both as graduate and

undergraduate courses.

• List members of HerCTI that are not enrolled in courses.

• Courses not offered in 2013 (i.e. no record of anybody being enrolled).



The ALL and ANY Operators

= ALL	<>ALL	= ANY	<> ANY
< ALL	$\leq = ALL$	< ANY	<= ANY
>ALL	>= ALL	> ANV	$\sim - \Lambda NV$

SELECT LastName, FirstName, SID FROM student WHERE started >= ALL (SELECT started FROM student);

Nesting Queries with ALL

- List the oldest studentgroup.
- List students belonging to the first student cohort.
- List courses that have a unique number.
- For all departments list the highest course number used by that department.

Naming Scope for nested assignments

Correlated Nesting Queries

List classes for which there is another class with the same name and a higher course number
List students that started at the university before some group they belong to was founded

Existence

Tests that a set is nonempty

SELECT LastName, FirstName, sid FROM student WHERE EXISTS (SELECT * FROM enrolled WHERE sid = studentID);

SELECT LastName, FirstName, sid FROM student WHERE NOT EXISTS (SELECT * FROM enrolled WHERE sid = studentID);

Unique Existence

Tests that a set contains one element

SELECT LastName, FirstName, sid FROM student WHERE UNIQUE (SELECT * FROM enrolled WHERE sid = studentID);

Not supported by Oracle, Access or SQLServer

Examples

• List students who have taken IT, but no CSC courses. • List students who have taken classes in CSC, IT and GPH.

• List student groups that have both graduate and undergraduate members.

• List courses in which nobody enrolled in 2013.

• List courses in which no student from Chicago ever enrolled.

CONTAINS

- List students who are members of all student groups.
 List students who have taken courses in all departments.
 List students who have enrolled in courses every year that courses were offered.